

4.5 Applications

1.) Write the equation of a sinusoid that rises from a minimum value of $y = 5$ at $x = 0$ to a max value of $y = 25$ at $x = 32$.

$$y = a \sin/\cos(b(x-c)) + d$$

$$d = 15$$

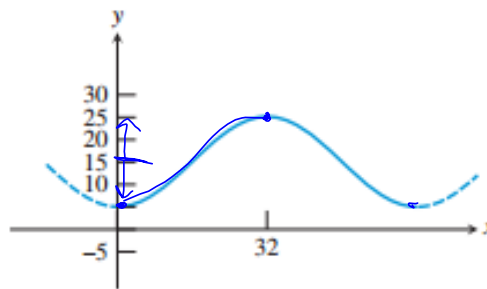
$$a = 10$$

$$-\cos$$

$$64 = \frac{2\pi}{b}$$

$$\frac{64b}{64} = \frac{2\pi}{64}$$

$$b = \frac{\pi}{32}$$



$$y = -10 \cos\left(\frac{\pi}{32}x\right) + 15$$

- 2.) Write a trigonometric model for the average daily temperature in Birmingham, Alabama.

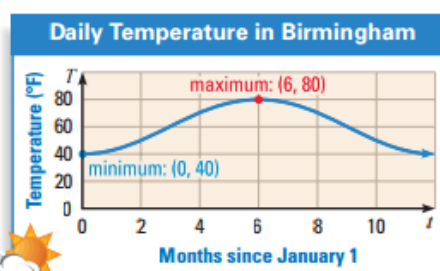
$$d = 60 \quad -\cos$$

$$a = 20$$

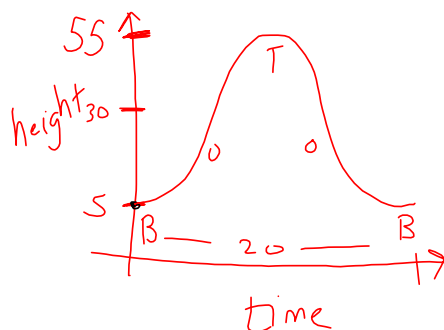
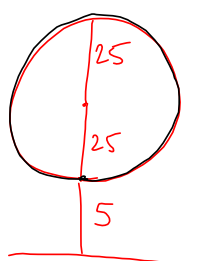
$$12 = \frac{2\pi}{b}$$

$$b = \pi/6$$

$$y = -20\cos\left(\frac{\pi}{6}x\right) + 60$$



3.) A ferris wheel with a radius of 25 feet is rotating at a rate of 3 revolutions per minute. When $t = 0$, a chair starts at the lowest point on the wheel, which is 5 feet above the ground. Write a model for the height h (in feet) of the chair as a function of the time t (in seconds).



$$d = 30$$

$$a = 25$$

$$p = 20 = \frac{2\pi}{b}$$

$$b = \frac{\pi}{10}$$

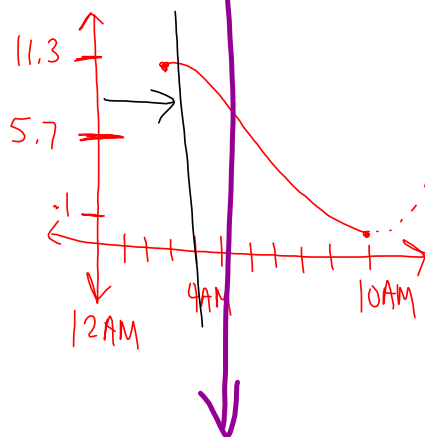
$$-\cos$$

$$h(t) = -25 \cos\left(\frac{\pi}{10}x\right) + 30$$

3.) Throughout the day, the depth at the end of a dock in Bar Harbor, Maine varies with the tides. At 4 A.M. the tide has a max of 11.3 feet and at 10 A.M., the tide is 0.1 feet.

8.5 ft 10.5 ft

- a.) Use a trigonometric function to model the data.
- b.) Find the depths at 9 A.M. and 3 P.M.
- c.) A boat needs at least 10 feet of water to motor at the dock. During what times in the afternoon can it safely dock?



$d = 5.7$ P.S.: 4
 $a = 5.6$
 + cos $12 = \frac{2\pi}{b}$
 $b = \frac{\pi}{6}$

$$y = 5.6 \cos\left(\frac{\pi}{6}(x-4)\right) + 5.7$$

14.7 → 17.3
 2:42 → 5:18

