

Pre-Calculus
Quiz Review: 3.1 – 3.3

Name KEY
Date _____ Block _____

Answer the following:

1.) An adult takes 400 mg of ibuprofen. Each hour, the amount of ibuprofen in the person's system decreases by about 29%.

a.) Write an exponential equation that models the situation.

$$y = 400(0.71)^x$$

b.) How much ibuprofen is left after 6 hours?

$$51.24 \text{ mg}$$

c.) How long until there is less than 1 milligram in the adult's system? (round to two decimal places)

$$17.49 \text{ hours}$$

2.) The foundation of your house has 1200 termites. The termite population grows at a rate of 2.4% per day.

a.) Write an exponential equation that models the situation.

$$y = 1200(1.024)^x$$

b.) How long does it take for the population of the termites to double? (round to two decimal places)

$$29.23 \text{ days}$$

$$\frac{y_2}{y_1} = 2$$

3.) Arsenic-74 is used to locate brain tumors. It has a half-life of 17.5 days.

a.) What is the decay factor? (round to four decimal places)

$$\left(\frac{1}{2}\right)^{1/17.5} \rightarrow (.9612)$$

b.) Write a half-life exponential function of a 90 mg sample.

$$y = 90\left(\frac{1}{2}\right)^{x/17.5}$$

c.) How much is left after 6 days?

$$70.96 \text{ mg}$$

d.) How many days will it take for there to be less than 50 milligrams present? (round to two decimal places)

$$14.84 \text{ days}$$

4.) The population of a town increases according to the model $P(t) = 2500e^{0.0293t}$, where t is the time in years, with t = 0 corresponding to 2000.

a.) Approximate the population in 2015 and 2025.

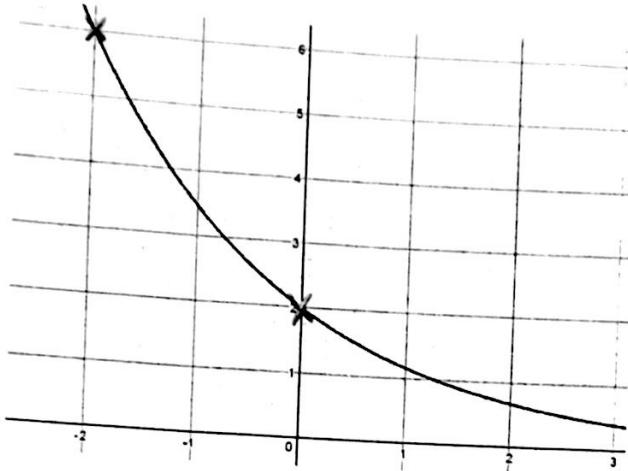
$$3879.83$$

$$5200.69$$

b.) How many years does it take for the population to break 15000? (round to two decimal places)

$$61.15 \text{ years}$$

5.) Write the equation of the exponential function in rational, radical, and decimal notation.



Rational: $y = 2 \left(\frac{1}{3}\right)^{\frac{x}{2}}$

Radical: $y = 2 \sqrt[1/3]{x}$

Decimal: (round to four decimal places):

$$y = 2(0.5774)^x$$

6.) Write the equation of the exponential function in rational, radical, and decimal notation.

| x | y |
|----|-------|
| -3 | 4.8 |
| 0 | 6 |
| 3 | 7.5 |
| 6 | 9.375 |

Rational:

$$y = 6 \left(\frac{5/4}{3}\right)^{x/3}$$

Radical:

$$y = 6 \sqrt[3]{5/4}^x$$

Decimal: (round to four decimal places):

$$y = 6(1.6772)^x$$

Evaluate each expression.

7.) $\log_9 81$

(2)

8.) $\log_{27} 3$

(1/3)

9.) $\log_2 32$

(5)

10.) $\log_8 1$

(0)

11.) $\ln e^4$

(4)

$$\log_e e^4$$

12.) $\log_8 2$

(1/3)

13.) $\log_3 \frac{1}{3}$

(-1)

14.) $\log_{\frac{1}{2}} 128$

(-7)

15.) $\log_4 2$

(1/2)

16.) $\log 1000$

(3)

17.) $\log_3 \frac{1}{243}$

(-5)

18.) $\log_{64} 4$

(1/3)

Expand each expression.

$$1.) \log_2(x^3 \cdot y^3)$$
$$\log_2 x^9 y^3$$
$$9\log_2 x + 3\log_2 y$$

$$20.) \log_3(z^4 \cdot \sqrt{x})$$

$$4\log_3 z + \frac{1}{2}\log_3 x$$

$$21.) \log_8\left(\frac{x^5}{y^4}\right) \quad \frac{x^5}{y^4}$$

$$5\log_8 x - 20\log_8 y$$

Condense each expression.

$$22.) 2\log x + 4\log y + 3\log z$$

$$\log x^2 y^4 z^3$$

$$23.) \log_2 12 + \log_2 7 + \log_2 5$$

$$\log_2 420$$

$$24.) 3\log_2 x + 15\log_2 y$$

$$\log_2 x^3 y^{15}$$

$$25.) 3\log_2 x - 6\log_2 y$$

$$\log_2 \frac{x^3}{y^6}$$

$$26.) \frac{1}{3}\log x + \frac{1}{3}\log y + \frac{1}{3}\log z$$

$$\log \sqrt[3]{xyz}$$